

PHILIPS

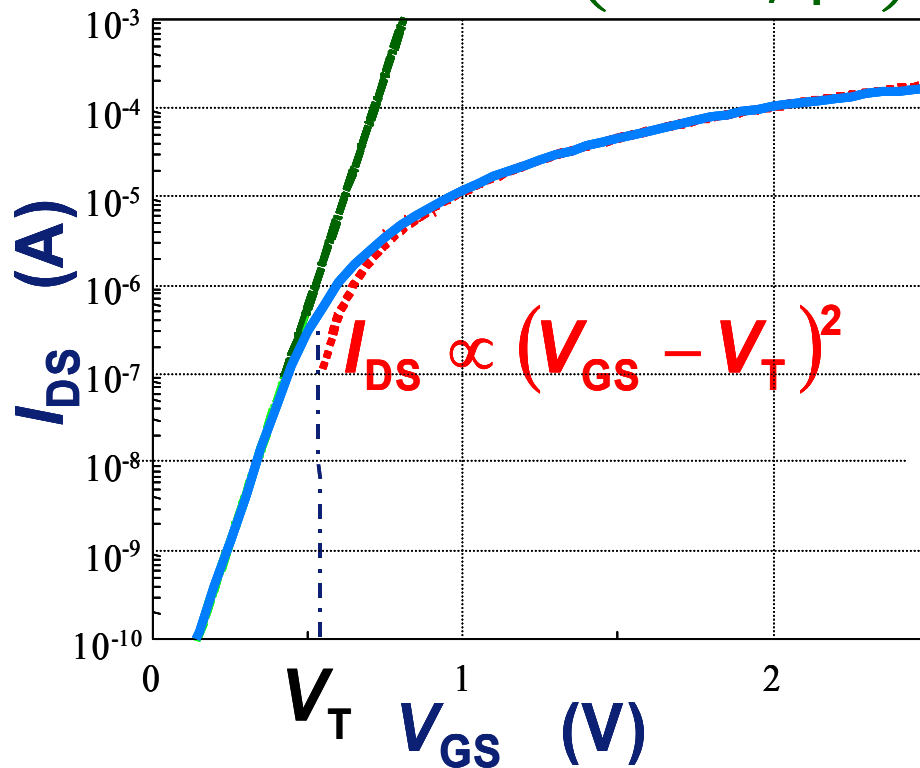
Surface-Potential versus Inversion-Charge Based Approaches to MOSFET Modeling

R. van Langevelde

Philips Research Laboratories
Eindhoven, The Netherlands

limitations V_T -based models (BSIM3/4, MM9)

$$I_{DS} \propto \exp\left(\frac{V_{GS} - V_T}{m \cdot \phi_T}\right)$$



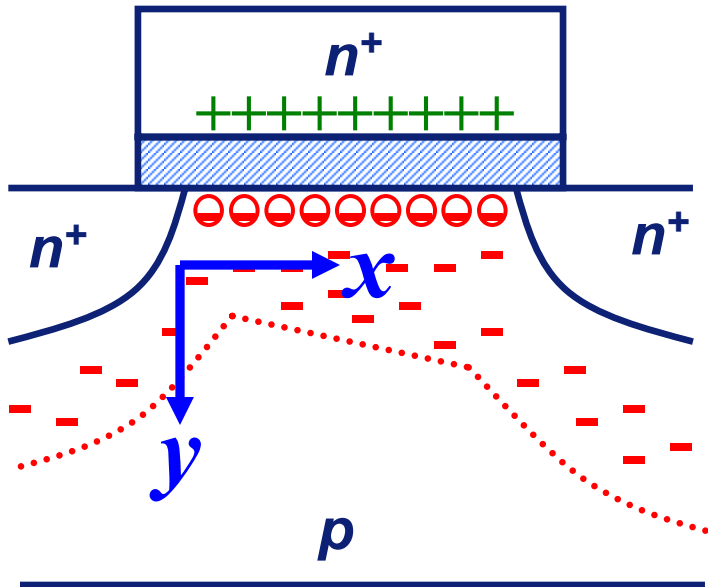
V_T -based models give inaccurate description of:

- moderate inversion
- drain/source symmetry
- accumulation

alternatives:

- ψ_s -based model
- Q_{inv} -based model

basis of MOSFET models: GCA



Poisson equation:

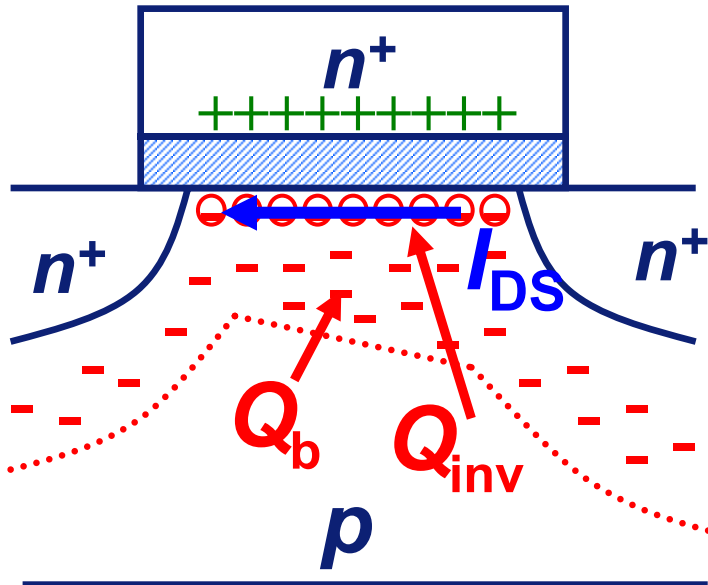
$$\frac{\partial^2 \psi}{\partial y^2} \approx - \frac{\rho}{\epsilon_{Si}}$$

all MOS models based on Gradual Channel Approximation (GCA)

→ equation in terms of surface potential ψ_s :

$$\left(\frac{V_{GB} - V_{FB} - \psi_s}{\gamma} \right)^2 = \psi_s + \phi_T \cdot e^{\frac{-\phi_B - V}{\phi_T}} \cdot \left(e^{\frac{\psi_s}{\phi_T}} - \frac{\psi_s}{\phi_T} - 1 \right) + \phi_T \cdot \left(e^{-\frac{\psi_s}{\phi_T}} - 1 \right)$$

basis of MOSFET models: CSA



drain-source current:

$$I_{DS} = -\mu \cdot \frac{W}{L} \cdot \int_{V_{SB}}^{V_{DB}} Q_{inv} \cdot dV$$

Charge Sheet
Approximation (CSA):

$$Q_{inv} = Q_{inv}(V_{GB}, \psi_s)$$

$$I_{DS} = I_{DS}(V_{GB}, \psi_{s0}, \psi_{sL})$$

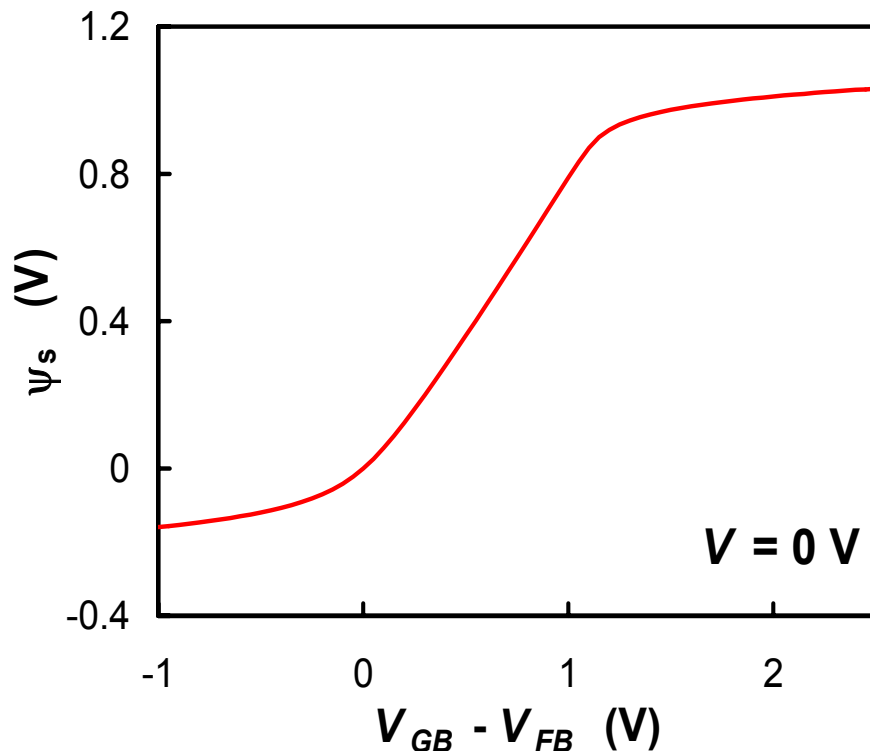
➔ surface-potential-based models

- further simplification by linearizing Q_{inv} w.r.t. ψ_s (leads to simple and robust equations)

surface-potential-based models

implicit equation for surface potential ψ_s (SPE):

$$\left(\frac{V_{GB} - V_{FB} - \psi_s}{\gamma} \right)^2 = \psi_s + \phi_T \cdot e^{\frac{-\phi_B - V}{\phi_T}} \cdot \left(e^{\frac{\psi_s}{\phi_T}} - \frac{\psi_s}{\phi_T} - 1 \right) + \phi_T \cdot \left(e^{\frac{-\psi_s}{\phi_T}} - 1 \right)$$



**extremely efficient
calculation of ψ_s :**

- analytical approximation
- iterative solution

**How to get to Q_{inv} -
based models?**

inversion-charge-based models: derivation

implicit equation for surface potential ψ_s (SPE):

$$\left(\frac{V_{GB} - V_{FB} - \psi_s}{\gamma} \right)^2 = \psi_s + \phi_T \cdot e^{\frac{-\phi_B - V}{\phi_T}} \cdot \left(e^{\frac{\psi_s}{\phi_T}} - \frac{\psi_s}{\phi_T} - 1 \right) + \phi_T \cdot \left(e^{-\frac{\psi_s}{\phi_T}} - 1 \right)$$

Q_{inv} -based models:

Q_{inv} -based models: derivation

implicit equation for surface potential ψ_s (SPE):

$$\left(\frac{V_{GB} - V_{FB} - \psi_s}{\gamma} \right)^2 = \psi_s + \varphi_T \cdot e^{\frac{\psi_s - \varphi_B - V}{\varphi_T}}$$

Q_{inv} -based models:

- neglect accumulation

Q_{inv} -based models: derivation

implicit equation for surface potential ψ_s (SPE):

$$V_{GB} - V_{FB} - \varphi_B - V = -\frac{Q_{inv} + Q_b}{C_{ox}} + \varphi_T \cdot \ln \left[\frac{Q_{inv} \cdot (Q_{inv} + 2 \cdot Q_b)}{\gamma^2 \cdot C_{ox}^2 \cdot \varphi_T} \right]$$

Q_{inv} -based models:

- neglect accumulation
- rewrite to Q_{inv} and Q_b (using CSA)

Q_{inv} -based models: derivation

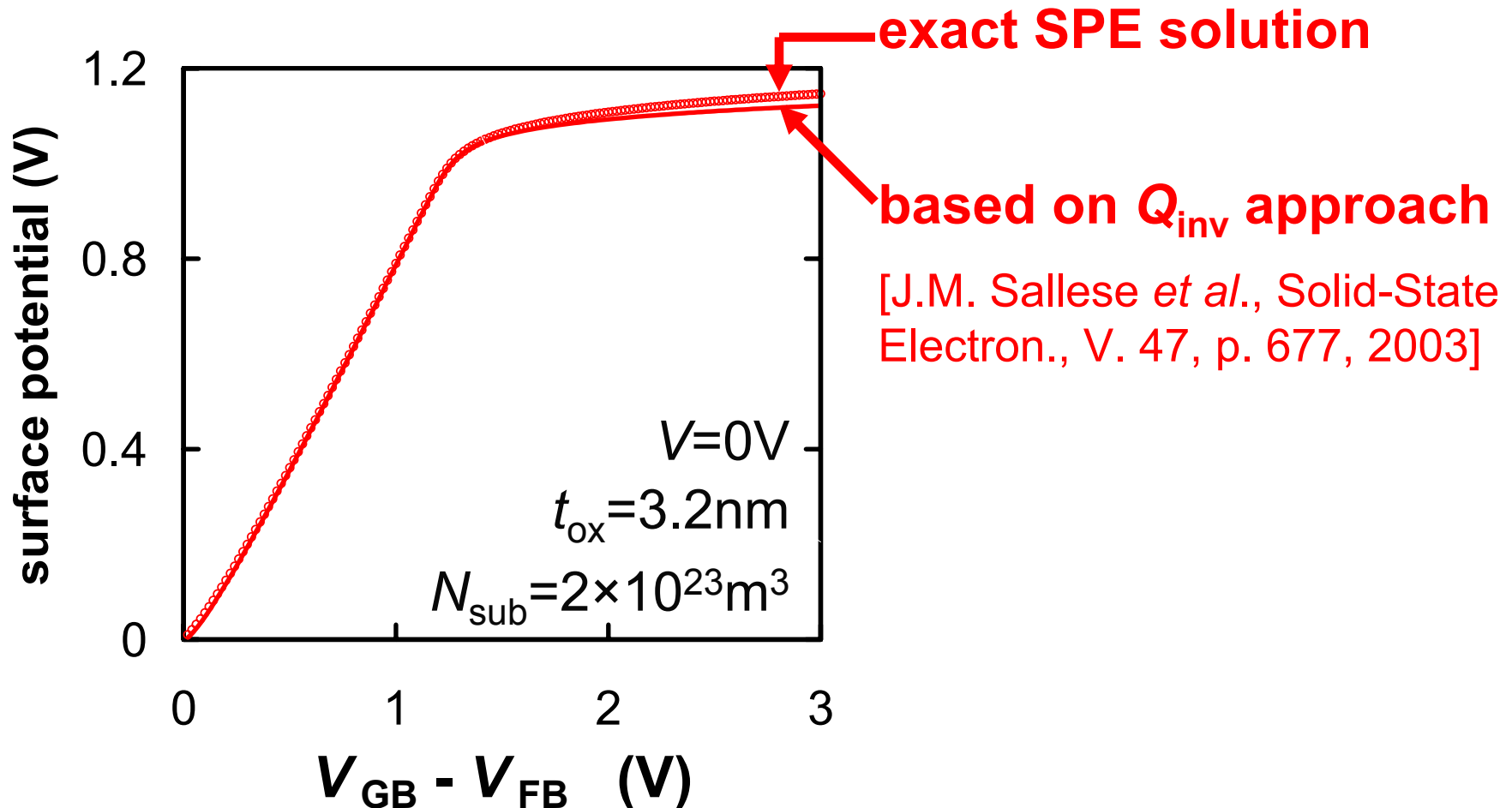
implicit relation for inversion charge Q_{inv} :

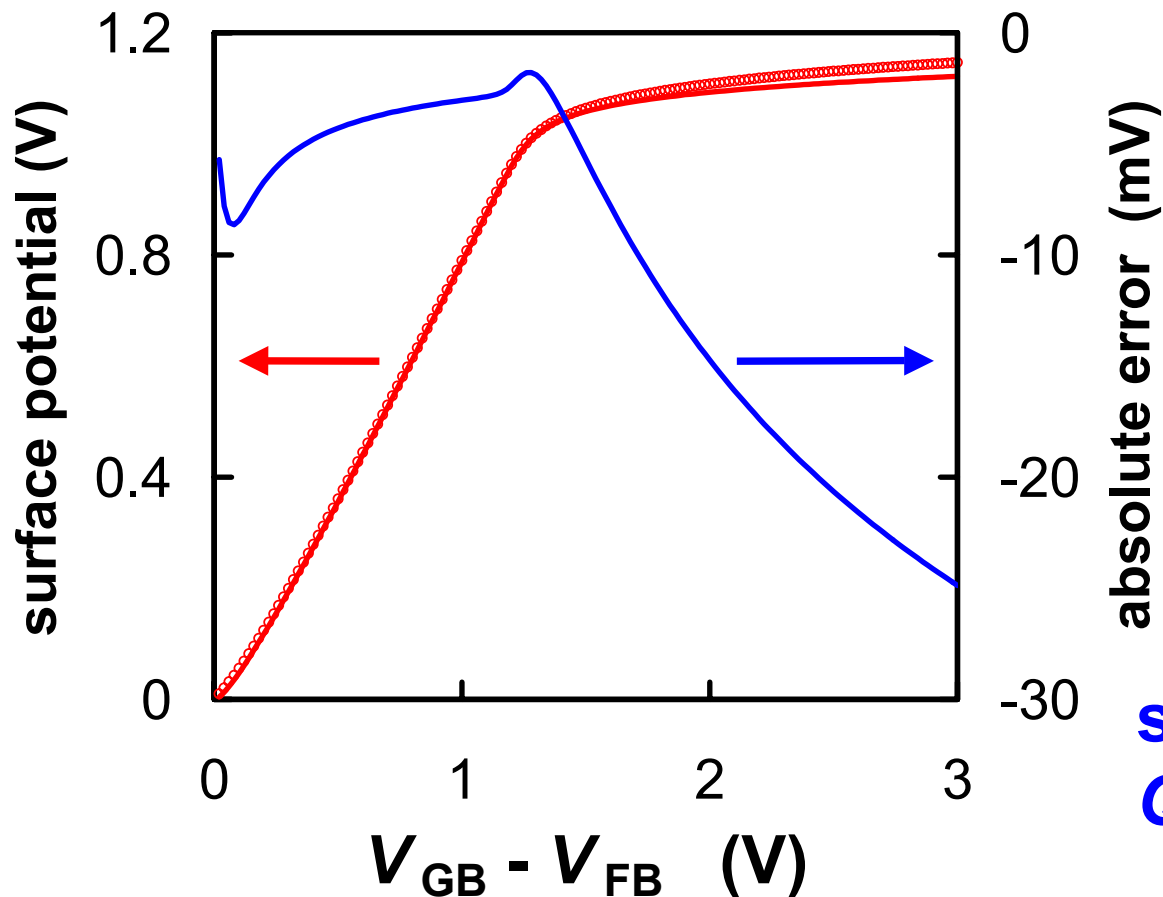
$$\frac{V_{GB} - V_{FB} - \phi_B - V - n_1}{n} \approx -\frac{Q_{inv}}{n \cdot C_{ox}} + \varphi_T \cdot \ln \left[\frac{-Q_{inv}}{n \cdot C_{ox} \cdot \varphi_T} \right]$$

Q_{inv} -based models:

- neglect accumulation
- rewrite to Q_{inv} and Q_b (using CSA)
- linearize/approximate
(use n and n_1 : functions of V_{GB} and V)

simplifications at the expense of accuracy!

Q_{inv} -based models: calculation of ψ_s **surface potential calculated from Q_{inv} -based relation**

Q_{inv} -based models: calculation of ψ_s **surface potential calculated from Q_{inv} -based relation****significant error in Q_{inv} -based solution**

Q_{inv} -based models: reduction to V_T -based model

implicit relation for inversion charge Q_{inv} :

$$\frac{V_{GB} - V_{FB} - \phi_B - V - n_1}{n} \approx -\frac{Q_{inv}}{n \cdot C_{ox}} + \phi_T \cdot \ln \left[\frac{-Q_{inv}}{n \cdot C_{ox} \cdot \phi_T} \right]$$

Q_{inv} -based models:

- neglect accumulation
- rewrite to Q_{inv} and Q_b (using CSA)
- linearize/approximate (use n and n_1)

Q_{inv} -based models: reduction to V_T -based model

implicit relation for inversion charge Q_{inv} :

$$Q_{inv} = -n \cdot C_{ox} \cdot \varphi_T \cdot W \left[\frac{V_{GB} - V_{FB} - n \cdot (\varphi_B + V + n_1)}{n \cdot \varphi_T} \right]$$

Q_{inv} -based models:

- neglect accumulation
- rewrite to Q_{inv} and Q_b (using CSA)
- linearize/approximate (use n and n_1)
- Lambert W function $W[x]: w + \ln(w) = x$

Q_{inv} -based models: reduction to V_T -based model

implicit relation for inversion charge Q_{inv} :

$$Q_{inv} = -n \cdot C_{ox} \cdot \varphi_T \cdot W \left[\frac{V_{GB} - V_T - V}{n \cdot \varphi_T} \right]$$

 Q_{inv} -based models:

- **neglect accumulation**
- **rewrite to Q_{inv} and Q_b**
- **linearize/approximate**
- **Lambert W function $W(.)$**
- **insert threshold voltage V_T**

Q_{inv} -based models: reduction to V_T -based model

explicit relation for inversion charge Q_{inv} :

$$Q_{inv} = -n \cdot C_{ox} \cdot \phi_T \cdot \ln \left[1 + \exp \left(\frac{V_{GB} - V_T - V}{n \cdot \phi_T} \right) \right]$$

Q_{inv} -based models:

- neglect accumulation
- rewrite to Q_{inv} and Q_b
- linearize/approximate
- Lambert W function $W(.)$
- insert threshold voltage V_T
- replace $W(.)$ by smoothing function

ψ_s -based versus Q_{inv} -based models

ψ_s -based model:

Poisson eq. + Gauss' law



GCA

surface potential equation



SCA
(linearize Q_{inv})

terminal currents & charges

Q_{inv} -based model:

Poisson eq. + Gauss' law



GCA

surface potential equation



accumulation
SCA
linearize Q_{inv}
approximate

inversion charge equation



terminal currents & charges

ψ_s -based versus Q_{inv} -based models

computational complexity:

ψ_s -based model: $(a - b \cdot x)^2 = x + c \cdot (e^x - x - 1) + e^{-x} - 1$



Q_{inv} -based model: $a = x + \ln(x)$

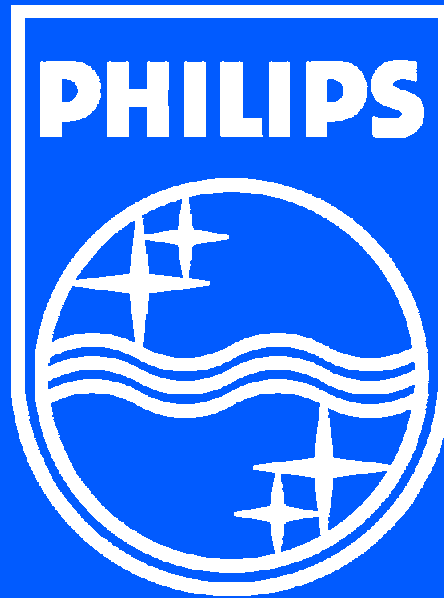
Q_{inv} -based eq. looks simpler than ψ_s -based eq.,
however:

- Q_{inv} -based eq. is not sufficient, needs to be extended to accumulation region (increasing complexity)
- calculation time of ψ_s or Q_{inv} small fraction of total calculation time

conclusions

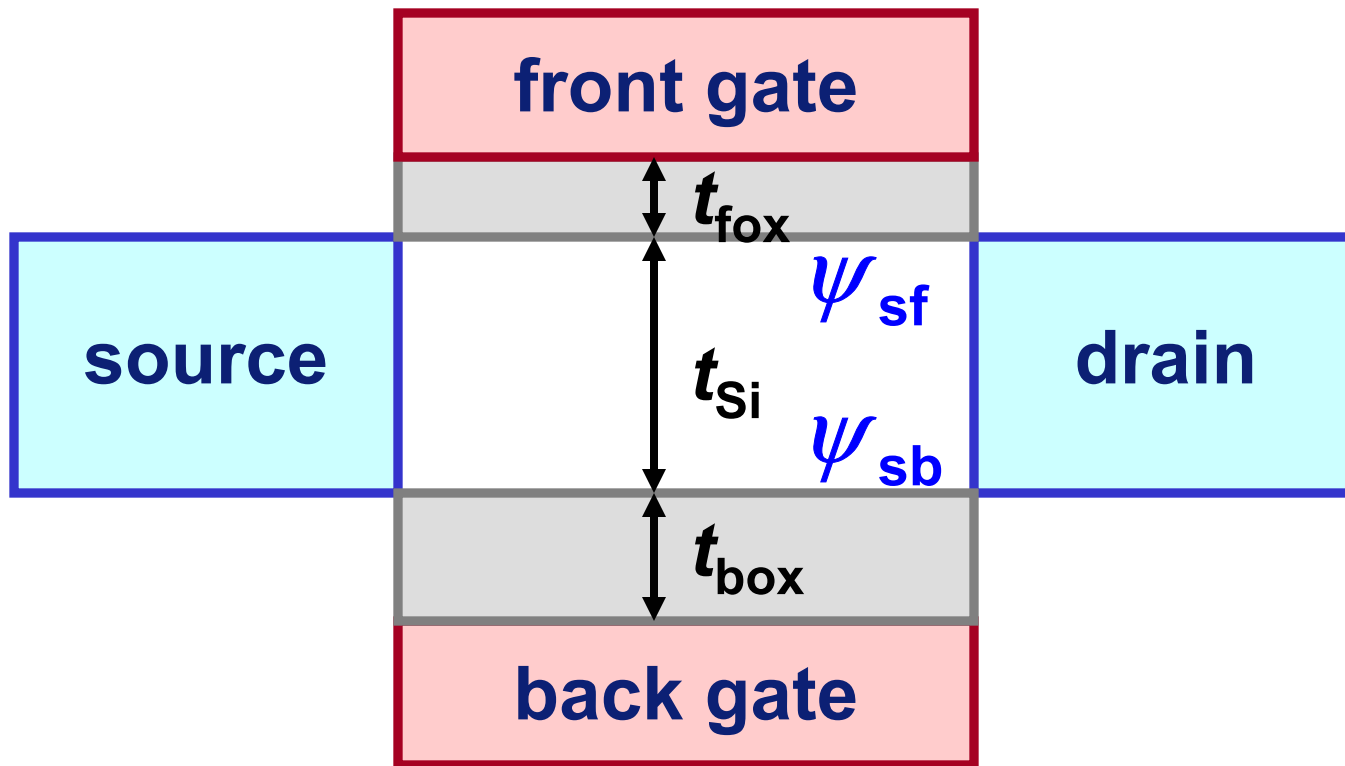
- Q_{inv} -based model is an approximation of ψ_s -based model
- drawbacks of Q_{inv} -based models:
 - less physical than ψ_s -based models
 - no accumulation included (varactor, overlap regions)
 - ψ_s is needed for gate current & charge

ψ_s -based model is best choice for a compact MOSFET model



multiple-gate (MG) devices

compact model for MG devices should be based on ψ_s



ψ_s -based model for double gate devices

MG devices: ψ_s -based model

surface potential is key to compact model

